Assembly: Introduction.

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Floats: Review

Normalized: exp field Normalized: frac field Normalized/denormalized

Special cases

Floats: Mastery

Normalized number bitstring to real number it represents Floating point multiplication Properties of floating point

Instruction set architectures

why are instruction set architectures important 8-bit vs. 16-bit. vs. 32-bit vs. 64-bit CISC vs. RISC

Looking ahead

Class plan

- 1. Today, Tuesday, 2/23: Bits to floats. Introduction to the software-hardware interface.
- 2. Reading assignment for next four weeks: CS:APP Chapter 3.
- 3. Thursday, 2/25: Programming Assignment 3 on bits, bytes, integers, floats out.
- 4. Monday, 3/1: Programming Assignment 2 due. Be sure to test on ilab, "make clean". Quiz 6 on floating point trickiness out.

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Floating point numbers

Avogadro's number

 $+6.02214 \times 10^{23} \, mol^{-1}$

Scientific notation

- sign
- mantissa or significand
- exponent

Floats and doubles

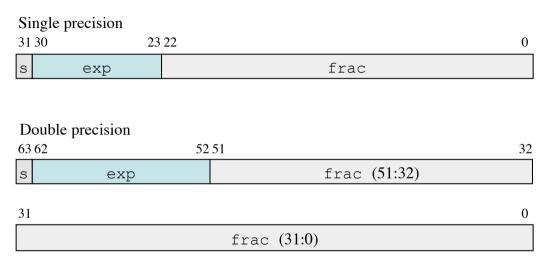


Figure: The two standard formats for floating point data types. Image credit CS:APP

Floats and doubles

property	float	double
total bits	32	64
s bit	1	1
exp bits frac bits	8	11
frac bits	23	52
C printf() format specifier	"%f"	''%lf''

Table: Properties of floats and doubles

The IEEE 754 number line

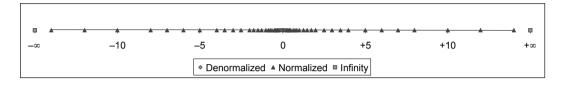


Figure: Full picture of number line for floating point values. Image credit CS:APP

$$+1.0/INF = +0; -1.0/INF = -0$$

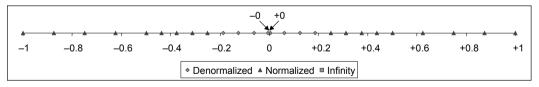


Figure: Zoomed in number line for floating point values. Image credit CS:APP

Different cases for floating point numbers

Value of the floating point number = $(-1)^s \times M \times 2^E$

- E is encoded the exp field
- ► *M* is encoded the frac field

Normalized	
s ≠0 & ≠255	f
Denormalized	
s 0 0 0 0 0 0 0 0	f
3a. Infinity	
s 1 1 1 1 1 1 1 1	000000000000000000000
3b. NaN	
OD. INDIA	-
s 1 1 1 1 1 1 1 1 1	≠ 0

Figure: Different cases within a floating point format. Image credit CS:APP

Normalized and denormalized numbers

Two different cases we need to consider for the encoding of E, M $_{\odot}$ $_{\odot}$

Normalized: exp field

For normalized numbers, $0 < \exp < 2^k - 1$

▶ exp is a *k*-bit unsigned integer

Bias

- need a bias to represent negative exponents
- \triangleright bias = $2^{k-1} 1$
- ▶ bias is the *k*-bit unsigned integer: 011..111

For no	rmalized	num	bers,
E = exp	o-bias		

In other words, exp = E + bias

property	float	double
k	8	11
bias	127	1023
smallest E (greatest precision)	-126	-1022
largest E (greatest range)	127	1023

Table: Summary of normalized exp field

Normalized: frac field

M = 1.frac

Floats: Summary

	normalized	denormalized
value of number	$(-1)^s \times M \times 2^E$	$(-1)^s \times M \times 2^E$
E	E = exp-bias	E = -bias + 1
bias	$2^{k-1}-1$	$2^{k-1}-1$
exp	$0 < exp < (2^k - 1)$	exp = 0
\dot{M}	M = 1.frac	M = 0.frac
	M has implied leading 1	M has leading 0
	greater range large magnitude numbers denser near origin	greater precision small magnitude numbers evenly spaced

Table: Summary of normalized and denormalized numbers

Floats: Special cases

number class	when it arises	exp field	frac field
+0 / -0		0	0
<pre>+infinity / -infinity</pre>	overflow or division by 0	$2^{k} - 1$	0
NaN not-a-number	illegal ops. such as $\sqrt{-1}$, inf-inf, inf*0	$2^{k}-1$	non-0

Table: Summary of special cases

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Normalized number bitstring to real number it represents

- ► Tiny FP: 1-bit s, 4-bit exp, 3-bit frac
- ▶ What does this encode: 1_1001_101
- ► s=1, so positive? negative? Negative number
- $ightharpoonup \exp = 1001_2 = 8+1 = 9$
- bias = $2^{k-1} 1 = 2^{4-1} 1 = 7$
- ightharpoonup E = exp-bias = 9-7 = 2
- frac = 101_2
- M = 1.frac $= 1.101_2$

How to multiply scientific notation?

Avagadro number squared?

$$(+6.02*(+6.02))(10^23)*(10^23) = (+6.02*(+6.02))*10^46$$

 $\sim = +36.0*10^46$
 $= +3.60*10^47$

Recall: $log(x \times y) = log(x) + log(y)$

Floating point multiplication

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FP Multiplication

```
■ (-1)<sup>s1</sup> M1 2<sup>E1</sup> x (-1)<sup>s2</sup> M2 2<sup>E2</sup>
```

■ Exact Result: (-1)^s M 2^E

• Sign s: $s1 ^ s2 = s1 \times S2 = s1 + s2 \pmod{2}$

Significand M: M1 x M2Exponent E: E1 + E2

Fixing

- If M ≥ 2, shift M right, increment E
- If E out of range, overflow
- Round M to fit frac precision

Implementation

Biggest chore is multiplying significands



Properties of floating point

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Mathematical Properties of FP Add

■ Compare to those of Abelian Group

Closed under addition? Yes

But may generate infinity or NaN

Commutative? Yes

Associative?

Overflow and inexactness of rounding

 \bullet (3.14+1e10)-1e10 = 0, 3.14+(1e10-1e10) = 3.14

0 is additive identity?

Every element has additive inverse? Yes

Yes, except for infinities & NaNs
 Almost

Monotonicity

■ $a \ge b \Rightarrow a+c \ge b+c$? Almost

Except for infinities & NaNs

Properties of floating point

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Mathematical Properties of FP Mult

■ Compare to Commutative Ring

Closed under multiplication?

Yes

But may generate infinity or NaN

Yes

• Multiplication Commutative? • Multiplication is Associative?

No

Possibility of overflow, inexactness of rounding

• Ex: (1e20*1e20) *1e-20= inf, 1e20* (1e20*1e-20) = 1e20

1 is multiplicative identity?

Yes

• Multiplication distributes over addition?

Nο

Possibility of overflow, inexactness of rounding

• 1e20*(1e20-1e20) = 0.0, 1e20*1e20 - 1e20*1e20 = NaN

Monotonicity

■ $a > b & c > 0 \Rightarrow a * c > b *c?$

Almost

Except for infinities & NaNs



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Computer organization

Layer cake

- Society
- Human beings
- Applications
- Algorithms
- ► High-level programming languages
- Interpreters
- Low-level programming languages
- Compilers
- Architectures
- Microarchitectures
- Sequential/combinational logic
- **Transistors**
- Semiconductors
- Materials science

Python, Java

why are instruction set architectures important

Interface between computer science and electrical and computer engineering

- Software is varied, changes
- ► Hardware is standardized, static

Computer architect Fred Brooks and the IBM 360

- ► IBM was selling computers with different capacities,
- ► Compile once, and can run software on all IBM machines.
- Backward compatibility.
- An influential idea.

CISC vs. RISC

Complex instruction set computer

- ▶ Intel and AMD
- ► Have an extensive and complex set of instructions
- ► For example: x86's extensions: x87, IA-32, x86-64, MMX, 3DNow!, SSE, SSE2, SSE3, SSSE3, SSE4, SSE4.2, SSE5, AES-NI, CLMUL, RDRAND, SHA, MPX, SGX, XOP, F16C, ADX, BMI, FMA, AVX, AVX2, AVX512, VT-x, VT-d, AMD-V, AMD-Vi, TSX, ASF
- Can license Intel's compilers to extract performance
- Secret: inside the processor, they break it down to more elementary instructions

CISC vs. RISC

Reduced instruction set computer

- MIPS, ARM, RISC-V (can find Patterson and Hennessy Computer Organization and Design textbook in each of these versions), an PowerPC
- ► Have a relatively simple set of instructions
- ► For example: ARM's extensions: SVE;SVE2;TME; All mandatory: Thumb-2, Neon, VFPv4-D16, VFPv4 Obsolete: Jazelle
- ► ARM: smartphones, Apple ARM M1 Mac

$$[1, 2, 4, 5, \dots 9] * 2 = [2, 4...]$$

Into the future: Post-ISA world

Post-ISA world

- ► Increasingly, the CPU is not the only character
- ► It orchestrates among many pieces of hardware
- ► Smartphone die shot
- ► GPU, TPU, FPGA, ASIC

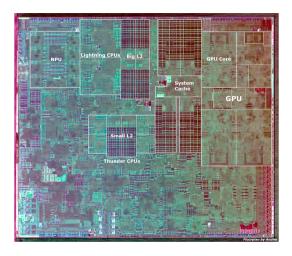


Figure: Apple A13 (2019 Apple iPhone 11 CPU). Image credit AnandTech