Caches: PA5 part 2, cache friendly code, digital logic

Yipeng Huang

Rutgers University

April 15, 2021

Announcements

PA5: Optimizing programs for caches

Cache-friendly code

Loop interchange

Cache blocking

Cache oblivious algorithms

Looking ahead

Class plan

- 1. PA5 now out. Due Monday, 4/26.
- 2. Short quiz 8 now out. Due Monday, 4/19.
- 3. Digital logic. Reading assignment: CS:APP Chapter 4.2. Recommended reading: Patterson & Hennessy, Computer organization and design, appendix on "The Basics of Logic Design." Available online via Rutgers Libraries.

Announcements

PA5: Optimizing programs for caches

Cache-friendly code

Loop interchange

Cache blocking

Cache oblivious algorithms

PA5: Optimizing programs for caches

Optimize some code for better cache performance

- 1. cacheBlocking
- 2. cacheOblivious

PA5: Optimizing programs for caches

A tour of files in the package

- ▶ Baseline implementations: matMul, matTrans.
- ▶ Your optimized implementations: cacheBlocking, cacheOblivious.
- ▶ What the autograder.py does:
 - 1. Testing for correctness.
 - 2. Getting the memory trace.
 - 3. Comparing your performance against the baseline.

Announcements

PA5: Optimizing programs for caches

Cache-friendly code

Loop interchange

Cache blocking

Cache oblivious algorithms

Cache-friendly code

Algorithms can be written so that they work well with caches:

- ► Maximize hit rate.
- Minimize miss rate.
- Minimize eviction counts.

Do so by:

- ► Increasing spatial locality.
- Increasing temporal locality.

A few specific techniques:

- ► Loop interchange.
- ► Cache blocking.
- Cache-oblivious algorithm implementation.

Loop interchange

Refer to textbook slides on "Rearranging loops to improve spatial locality"

- ► Loop interchange increases spatial locality.
- ▶ In PA5, fourth part "cacheBlocking" you can explore the impact of this on matrix multiplication.
- ▶ In practice, programmers do not have to worry about this optimization.
- ➤ Optimized automatically in GCC by compiler flag -floop-interchange and -03.

Cache blocking

Refer to textbook slides on "Using blocking to improve temporal locality"

- Cache blocking increases temporal locality.
- ▶ In PA5, fourth part "cacheBlocking" you can explore the impact of this on matrix multiplication.
- ▶ In practice, programmers do not have to worry about this optimization.
- ▶ Optimized automatically in GCC by compiler flag -floop-block. But it is not part of default optimizations such as -03 so you have to remember to set it.

Cache oblivious algorithms

The challenge in writing code / compiling programs to take advantage of caches:

- ▶ Programmers do not easily have information about target machine.
- ▶ Compiling binaries for every envisioned target machine is costly.

Matrix transpose baseline algorithm: iteration

$$\mathbf{A} = \begin{bmatrix} a_{0,0} & a_{0,1} & a_{0,2} & a_{0,3} \\ a_{1,0} & a_{1,1} & a_{1,2} & a_{1,3} \\ a_{2,0} & a_{2,1} & a_{2,2} & a_{2,3} \\ a_{3,0} & a_{3,1} & a_{3,2} & a_{3,3} \end{bmatrix}$$
$$\mathbf{B} = \mathbf{A}^{\mathsf{T}} = \begin{bmatrix} a_{0,0} & a_{1,0} & a_{2,0} & a_{3,0} \\ a_{0,1} & a_{1,1} & a_{2,1} & a_{3,1} \\ a_{0,2} & a_{1,2} & a_{2,2} & a_{3,2} \\ a_{0,3} & a_{1,3} & a_{2,3} & a_{3,3} \end{bmatrix}$$

```
\mathbf{A} = \begin{bmatrix} a_{0,0} & a_{0,1} & a_{0,2} & a_{0,3} \\ a_{1,0} & a_{1,1} & a_{1,2} & a_{1,3} \\ a_{2,0} & a_{2,1} & a_{2,2} & a_{2,3} \\ a_{3,0} & a_{3,1} & a_{3,2} & a_{3,3} \end{bmatrix}
\begin{bmatrix} a_{0,0} & a_{0,1} & a_{0,2} & a_{0,3} \\ a_{1,0} & a_{1,1} & a_{1,2} & a_{1,3} \\ a_{2,0} & a_{2,1} & a_{2,2} & a_{2,3} \\ a_{3,0} & a_{3,1} & a_{3,2} & a_{3,3} \end{bmatrix}
\begin{bmatrix} a_{0,0} & a_{0,1} & a_{0,2} & a_{0,3} \\ a_{1,0} & a_{1,1} & a_{1,2} & a_{1,3} \\ a_{2,0} & a_{2,1} & a_{2,2} & a_{2,3} \\ a_{3,0} & a_{3,1} & a_{3,2} & a_{3,3} \end{bmatrix}
\begin{bmatrix} a_{1,0} & a_{1,1} & a_{1,2} & a_{1,3} \\ a_{2,0} & a_{2,1} & a_{2,2} & a_{2,3} \\ a_{3,0} & a_{3,1} & a_{3,2} & a_{3,3} \end{bmatrix}
\begin{bmatrix} a_{1,0} & a_{1,1} & a_{1,2} & a_{1,3} \\ a_{2,0} & a_{2,1} & a_{2,2} & a_{2,3} \\ a_{3,0} & a_{3,1} & a_{3,2} & a_{3,3} \end{bmatrix}
```

Matrix transpose via recursion

$$\mathbf{A} = \begin{bmatrix} A_{0,0} & A_{0,1} \\ A_{1,0} & A_{1,1} \end{bmatrix} = \begin{bmatrix} a_{0,0} & a_{0,1} & a_{0,2} & a_{0,3} \\ a_{1,0} & a_{1,1} & a_{1,2} & a_{1,3} \\ a_{2,0} & a_{2,1} & a_{2,2} & a_{2,3} \\ a_{3,0} & a_{3,1} & a_{3,2} & a_{3,3} \end{bmatrix}$$
$$\mathbf{B} = \mathbf{A}^{\mathsf{T}} = \begin{bmatrix} A_{0,0}^{\mathsf{T}} & A_{1,0}^{\mathsf{T}} \\ A_{0,1}^{\mathsf{T}} & A_{1,1}^{\mathsf{T}} \end{bmatrix} = \begin{bmatrix} a_{0,0} & a_{1,0} & a_{2,0} & a_{3,0} \\ a_{0,1} & a_{1,1} & a_{2,1} & a_{3,1} \\ a_{0,2} & a_{1,2} & a_{2,2} & a_{3,2} \\ a_{0,3} & a_{1,3} & a_{2,3} & a_{3,3} \end{bmatrix}$$

32x32 transpose -> 4 separate 16x16 transpose tasks

Strategy:

- Divide and conquer large matrix to transpose into smaller transpositions.
- After some recursion, problem will fit well inside cache capacity.
- Once enough locality exists withing subroutine, switch to plain iterative approach.

Advantages:

- ► No need to know about cache capacity and parameters beforehand.
- Works well with deep multilevel cache hierarchies: different amounts of locality for each cache level. 2 999 13/15

16x16 -> 4 separate 8x8

 $8x8 \rightarrow 4$ separate 4x4

Announcements

PA5: Optimizing programs for caches

Cache-friendly code

Loop interchange

Cache blocking

Cache oblivious algorithms

Memory hierarchy implications for software-hardware abstraction

It is not entirely true the architecture can hide details of microarchitecture Even less true going forward. What to do?

Application level recommendations

- Use industrial strength, optimized libraries compiled for target machine.
- Lapack, Linpack, Matlab, Python SciPy, NumPy...
- https://people.inf.ethz.ch/markusp/teaching/ 263-2300-ETH-spring11/slides/class08.pdf

Algorithm level recommendations

Deploy cache-oblivious algorithm implementations.

Compiler level recommendations

- Enable compiler optimizations—e.g., -03, -floop-interchange, -floop-block.
- https://gcc.gnu.org/onlinedocs/gcc/Optimize-Options.html