Quantum Computer Prototypes

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Course evaluation

https://sirs.ctaar.rutgers.edu/blue Very important to help develop next iteration of this course.
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   Essential hardware components of a quantum computer
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   Trapped ion quantum computers
   Superconducting quantum computers
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Essential hardware components of a quantum computer

Host processor plane

Control processor plane
digital processing, non-deterministic timing

Control and measurement plane
analog processing, deterministic timing

Quantum data plane

[National Academies of Sciences, Engineering, and Medicine, 2019, Chapter 5]
TU Delft control and measurement processors

Fig. 9. Quantum microarchitecture implementing the instantiated eQASM for the seven-qubit superconducting quantum processor.

**Figure:** Credit: [Fu et al., 2019]

This is an example for superconducting qubits.
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DiVincenzo’s criteria

The central challenge
Keeping qubits weakly coupled to external decoherence forces, while keeping them strongly coupled to each other.

Examples
The requirements are often conflicting: single nuclear spin can remain in a superposition state for days, but because it couples so weakly with the world, control and measurement is hard.
DiVincenzo’s criteria

1. A scalable physical system with well characterized qubits
2. The ability to initialize the state of the qubits to a simple fiducial state, such as $|000\ldots\rangle$
3. Long relevant decoherence times, much longer than the gate operation time
4. A “universal” set of quantum gates
5. A qubit-specific measurement capability
6. The ability to interconvert stationary and flying qubits
7. The ability to transmit faithfully flying qubits between specified locations
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Trapped ion quantum computers

Strengths
Long coherence, high inter-connectivity

Weaknesses
Rely on multiple interacting technologies, relatively slow (1–100µS) gate operation times

Examples
Research groups: University of Maryland, IonQ, Honeywell

Figure: Credit: [Ladd et al., 2010]

FIG. 2: Schematic of ion trap apparatus. Electric potentials are applied to appropriate electrodes in order to confine a 1-D crystal of individual atomic ions. Lasers affect coherent spin-dependent forces to the ions that can entangle their internal qubit levels through their Coulomb-coupled motion. Resonant lasers can also cause spin-dependent fluorescence for the efficient detection of the trapped ion qubit states. The inset shows a collection of atomic Ca⁺⁺ ions fluorescing (courtesy R. Blatt, University of Innsbruck).
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7. The ability to transmit faithfully flying qubits between specified locations
Ion traps: A scalable physical system with well characterized qubits

Optical qubits
Ground electronic state and a metastable excited electronic state. Large gap, higher frequency, optical laser for control.

Hyperfine qubits
Pair of energy states resulting from nucleus with non-zero spin with smaller energy difference. Small gap, lower frequency, microwave sources for control.

Figure:
Credit: [National Academies of Sciences, Engineering, and Medicine, 2019]
Ion traps: A scalable physical system with well characterized qubits

**Optical qubits**
Ground electronic state and a metastable excited electronic state. Large gap, higher frequency, optical laser for control.

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Pair of energy states resulting from nucleus with non-zero spin with smaller energy difference. Small gap, lower frequency, microwave sources for control.

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Figure:
Credit: [Nielsen and Chuang, 2011]
Ion traps: Long relevant decoherence times, much longer than the gate operation time

High vacuum

Radio frequency Paul trap
Like a rotating saddle. RF at 20–200 MHz. Voltage amplitudes 30–400 V.

Direct current axial trap
DC axial trap 0-30V

Figure: Credit: NAP.
Ion traps: Long relevant decoherence times, much longer than the gate operation time

An artificial 1 dimensional crystal

Once ions are settled in trap, confined in two dimensions with more freedom to move axially. They repel and interact with each other due to Coulomb repulsion.

**Figure:** Credit: NAP.
Ion traps: The ability to initialize the state of the qubits to a simple fiducial state, such as $|000\ldots\rangle$.

Cooling the ions down to ground state

Continuous wave lasers carry away momentum from system.
Ion traps: A “universal” set of quantum gates

Coherent qubit control system

Single qubit gates
Rabi oscillations between the two qubit levels with resonant laser pulses.

![Figure: Rabi oscillations of a single Ca$^+$ ion. Each dot represents 1000 experiments, each consisting of initialization, application of laser light on the qubit transition and state detection. Credit: [Häffner et al., 2008]](image)

**Figure:** Credit: [Häffner et al., 2008]
Ion traps: A “universal” set of quantum gates

Two qubit gates

2. Ignacio Cirac and Peter Zoller two qubit gate in 1995.
4. Global entangling gate, or pair-wise control signals.
5. 2–5% error rates for two-qubit gates.

Figure: Credit: [Häffner et al., 2008]
Ion traps: A qubit-specific measurement capability

1. Continuous wave lasers for read out illumination.
3. Photon detectors.

**Figure:** Credit: [Ladd et al., 2010]

*FIG. 2: Schematic of ion trap apparatus. Electric potentials are applied to appropriate electrodes in order to confine a 1-D crystal of individual atomic ions. Lasers affect coherent spin-dependent forces to the ions that can entangle their internal qubit levels through their Coulomb-coupled motion. Resonant lasers can also cause spin-dependent fluorescence for the efficient detection of the trapped ion qubit states. The inset shows a collection of atomic Ca$^+$ ions fluorescing (courtesy R. Blatt, University of Innsbruck).*
Ion traps: The ability to interconvert stationary and flying qubits

1. Each trap may scale to over 50 qubits.
2. Proposals to couple distant traps via photonics or via entangled ions.
Ion traps: The ability to transmit faithfully flying qubits between specified locations

**Figure 4.2:** (a) The physical structure of an ion-trap quantum computer. An optimistic size of the trapping electrodes is in the order of tens of micrometers [193]. The data ion is kept together with a cooling ion and cooled before and after each movement step or logic gate. The ion-group can move to any of the 6 adjacent trapping regions for interaction with another ion-group. (b) A two-qubit gate sequence where the ion-group in the top left junction moves to the middle for a two-qubit gate. The gate is implemented with an external laser beam acting on the two ion-groups.

*Figure: Ion shuttling. Credit: [Metodi and Chong, 2006]*
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Superconducting quantum computers

**Strengths**
Solid state, lithographically defined (single mask, single metal layer), relatively fast (10–100nS) gate operation times

**Weaknesses**
Variability, cryogenic

**Examples**
Research groups: IBM, Google (Bristlecone, Sycamore), Rigetti
DiVincenzo’s criteria

1. A scalable physical system with well characterized qubits
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**Superconductors: A scalable physical system with well characterized qubits**

![Circuit diagrams](Figure)

**Figure.** Credit: [Krantz et al., 2019]

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**Linear resonator**

Superconducting resonator

\[ H = \frac{\Phi^2}{2L} + \frac{Q^2}{2C} \]

\[ H = \hbar \omega_0 (n + \frac{1}{2}) \]

\[ \omega_0 = \frac{1}{\sqrt{LC}} \]

C (capacitance acts as mass)

L (inductance) acts as spring

[Devoret et al., 2004]

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**Figure.** Credit: [Kraus et al., 2019]
Superconductors: A scalable physical system with well characterized qubits

Nonlinear resonator

1. Nonlinear inductor: Josephson junction.
2. Insulator sandwiched between two superconductors.
3. Al-AlOx-Al.
4. Josephson junction introduces nonlinearity.
5. Electrons pair up to form Cooper pairs, which allow them to tunnel across the insulator in discrete quanta.

Figure: Credit: wikimedia.org
Superconductors: A scalable physical system with well characterized qubits

![Circuit diagrams](image)

**Figure**: Credit: [Krantz et al., 2019]

Artificial atoms with atom-like spectra

Anharmonicity describes the difference between $\hbar \omega_{01}$ and $\hbar \omega_{12}$.

**Figure Caption**: [Kraus et al., 2019]
Superconductors: Long relevant decoherence times, much longer than the gate operation time

Superconductors and cryogenic temperatures needed for qubit coherence

1. Superconductivity eliminates heat dissipation with current.
2. Cryogenic temperatures eliminate state transitions due to thermal excitation (5GHz microwave corresponds to thermal energy of 250mK).
3. Cryogenic temperatures also needed for superconductivity (for aluminium, $T_c = 1.2$K).
Superconductors: Long relevant decoherence times, much longer than the gate operation time

Dilution refrigerator

1. Dry refrigerator cools to 50K and 3K. Here, thermal budget is 1W.
2. Liquid helium cools to 700mK, 50mK, 10mK. Here, thermal budget is $30\mu W–1\text{mW}$.

Cryogenic signal processing stage-by-stage

1. Thermally resistive will necessarily imply electrically lossy.
2. Filter out the noise.
3. Attenuate to send to next stage.

Takes 2 days to cool down to operating temperature.
Superconductors: A “universal” set of quantum gates

**Single qubit gates**

1. JJ reshapes the parabolic energy well so that gap between lower energy levels is wider.
2. Creates a $f_{01}$ transition frequency.
3. Then you can change the state $(I,V)$ by injecting microwaves at the right frequency.
4. $\approx 5$GHz microwaves stimulate transition, with standard deviation $\sigma \approx 150$MHz.

**Figure:** Credit: [Krantz et al., 2019]
Superconductors: A “universal” set of quantum gates

Figure: Credit: [Ding and Chong, 2020, Chapter 2.4.2]

**Figure 2.12:** **Left:** Qubit frequencies as a function of external magnetic flux. The first three levels of the transmon, $\omega_{01}$ and $\omega_{12}$, are plotted. **Right:** Circuit diagram for a frequency-tunable (asymmetric) transmon qubit (highlighted in black), consisting of a capacitor and two asymmetric Josephson junctions. Highlighted in gray are two control lines: the external magnetic flux control $\phi$ and microwave voltage drive line $V_d(t)$ for each transmon qubit.
Superconductors: A "universal" set of quantum gates

Figure 2.13: Two-qubit interactions for two capacitively coupled transmons. **Left:** Two-qubit gates are implemented with resonance of qubit frequencies. Shown here are how qubit frequencies are tuned for $i$SWAP gate and $CZ$ gate. **Right:** Circuit diagram of two capacitively coupled transmon qubits.

Figure: Credit: [Ding and Chong, 2020, Chapter 2.4.2]
Superconductors: A “universal” set of quantum gates

Native two qubit gates

1. iSWAP
2. CZ
3. CR

Frequency allocation

1. Single junction nontunable
2. Two-junction tunable

Examples

OpenPulse.
Superconductors: A qubit-specific measurement capability

- Dispersive readout
- State-dependent frequency shift of a resonator coupled to each qubit [Ding and Chong, 2020, Chapter 2.4.2]
Superconducting quantum computers

**Strengths**
Solid state, lithographically defined (single mask, single metal layer), relatively fast (10–100nS) gate operation times

**Weaknesses**
Variability, cryogenic, CMOS processes for superconducting circuit and peripheral circuitry not compatible, limited physical volume in cryostat

**Examples**
Research groups: IBM, Google (Bristlecone, Sycamore), Rigetti
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Trapped ions and superconductors are currently the only technologies with full-stack integration.

In fact, it is quite remarkable that both are at comparable maturity level, given the wildly different technologies involved.

Outside of TI and SC, other technologies are demonstrating single and two qubit gates.
Other technologies

Atomic, molecular, and optical physics
Trapped optical ion, trapped (hyperfine) microwave/RF ion, trapped neutral atoms, liquid nuclear magnetic resonance.

Solid-state
GaAs quantum dot, optically active defects, diamond defects, nitrogen vacancy centers, superconducting phase/charge/flux qubit.

All are in infancy.
Hard to bet on long term winner.
### Other technologies

<table>
<thead>
<tr>
<th>Type of Matter Qubit</th>
<th>Coherence</th>
<th>Benchmarking</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$\omega_0/2\pi$</td>
<td>$T_2$</td>
</tr>
<tr>
<td>Trapped Optical Ion $^{40}\text{Ca}^+$</td>
<td>400 THz</td>
<td>1 ms</td>
</tr>
<tr>
<td>Trapped Microwave Ion $^{9}\text{Be}^+$</td>
<td>300 MHz</td>
<td>10 sec</td>
</tr>
<tr>
<td>Trapped Neutral Atoms $^{87}\text{Rb}$</td>
<td>7 GHz</td>
<td>3 sec</td>
</tr>
<tr>
<td>Liquid Molecule Nuclear Spins $^{28}$</td>
<td>500 MHz</td>
<td>2 sec</td>
</tr>
<tr>
<td>e$^-$ Spin in GaAs Quantum Dot $^{29,31}$</td>
<td>10 GHz</td>
<td>3 $\mu$s</td>
</tr>
<tr>
<td>e$^-$ Spins Bound to $^{31}\text{P}:^{28}\text{Si}$ $^{32,33}$</td>
<td>10 GHz</td>
<td>60 ms</td>
</tr>
<tr>
<td>Nuclear Spins in Si $^{34}$</td>
<td>60 MHz</td>
<td>25 sec</td>
</tr>
<tr>
<td>NV$^-$ Center in Diamond $^{35,37}$</td>
<td>3 GHz</td>
<td>2 ms</td>
</tr>
<tr>
<td>Superconducting Phase Qubit $^{38,40}$</td>
<td>10 GHz</td>
<td>350 ns</td>
</tr>
<tr>
<td>Superconducting Charge Qubit $^{41,43}$</td>
<td>10 GHz</td>
<td>2 $\mu$s</td>
</tr>
<tr>
<td>Superconducting Flux Qubit $^{44,45}$</td>
<td>10 GHz</td>
<td>4 $\mu$s</td>
</tr>
</tbody>
</table>

Table comparing the current performance of various matter qubits. The approximate resonant frequency of each qubit is listed as $\omega_0/2\pi$; this is not necessarily the speed of operation, but sets a limit for defining the phase of a single qubit. Therefore, $Q = \omega_0 T_2$ is a very rough quality factor. Benchmarking values show approximate error rates for single or multi-qubit gates. Values marked with * are found by state tomography, and give the departure of the fidelity from 100%. Values marked with † are found with randomized benchmarking. Other values are rough experimental gate error estimates.

**Figure:** Credit: [Ladd et al., 2010]
### Other technologies

<table>
<thead>
<tr>
<th>System</th>
<th>$\tau_Q$</th>
<th>$\tau_{op}$</th>
<th>$n_{op} = \lambda^{-1}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nuclear spin</td>
<td>$10^{-2} - 10^8$</td>
<td>$10^{-3} - 10^{-6}$</td>
<td>$10^5 - 10^{14}$</td>
</tr>
<tr>
<td>Electron spin</td>
<td>$10^{-3}$</td>
<td>$10^{-7}$</td>
<td>$10^4$</td>
</tr>
<tr>
<td>Ion trap (In$^+$)</td>
<td>$10^{-1}$</td>
<td>$10^{-14}$</td>
<td>$10^{13}$</td>
</tr>
<tr>
<td>Electron – Au</td>
<td>$10^{-8}$</td>
<td>$10^{-14}$</td>
<td>$10^6$</td>
</tr>
<tr>
<td>Electron – GaAs</td>
<td>$10^{-10}$</td>
<td>$10^{-13}$</td>
<td>$10^3$</td>
</tr>
<tr>
<td>Quantum dot</td>
<td>$10^{-6}$</td>
<td>$10^{-9}$</td>
<td>$10^3$</td>
</tr>
<tr>
<td>Optical cavity</td>
<td>$10^{-5}$</td>
<td>$10^{-14}$</td>
<td>$10^9$</td>
</tr>
<tr>
<td>Microwave cavity</td>
<td>$10^0$</td>
<td>$10^{-4}$</td>
<td>$10^4$</td>
</tr>
</tbody>
</table>

Figure 7.1. Crude estimates for decoherence times $\tau_Q$ (seconds), operation times $\tau_{op}$ (seconds), and maximum number of operations $n_{op} = \lambda^{-1} = \tau_Q/\tau_{op}$ for various candidate physical realizations of interacting systems of quantum bits. Despite the number of entries in this table, only three fundamentally different qubit representations are given: spin, charge, and photon. The ion trap utilizes either fine or hyperfine transitions of a trapped atom (Section 7.6), which correspond to electron and nuclear spin flips. The estimates for electrons in gold and GaAs, and in quantum dots are given for a charge representation, with an electrode or some confined area either containing an electron or not. In optical and microwave cavities, photons (of frequencies from gigahertz to hundreds of terahertz) populating different modes of the cavities represent the qubit. Take these estimates with a grain of salt: they are only meant to give some perspective on the wide range of possibilities.

**Figure: Credit: [Nielsen and Chuang, 2011]**
Other technologies

<table>
<thead>
<tr>
<th>Technology</th>
<th>Coherence Time (s)</th>
<th>1-Qubit Gate Latency (s)</th>
<th>2-Qubit Gate Latency (s)</th>
<th>1-Qubit Gate Fidelity (%)</th>
<th>2-Qubit Gate Fidelity (%)</th>
<th>Mobile</th>
</tr>
</thead>
</table>

Table 1. Metrics for various quantum technologies. * Nuclear/Electron Hybrid

Figure: Credit: [Resch and Karpuzcu, 2019]
Primary sources

- [National Academies of Sciences, Engineering, and Medicine, 2019, Chapter 5, Appendix B, Appendix C]
- [DiVincenzo, 2000]
- [Nielsen and Chuang, 2011, Chapter 1.5]
- [Nielsen and Chuang, 2011, Chapter 7]
- [Marinescu, 2011, Chapter 6]
*arXiv preprint cond-mat/0411174*.


