C Programming: Debugging, Bits, Bytes, Integers

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bstLevelOrder.c: Level order traversal of a binary search tree

Binary search tree: BSTNode, insert(), delete()

Linked list implementation of a queue: QueueNode, Queue, enqueue(), dequeue() Challenges in CS programming assignments, strategies to get unstuck, resources

In CS 111, 112, 211, what are reasons programming assignments are challenging?

- ► Not sure where to start.
- It isn't working.
- The CS 211 teachers say that knowing Java helps programming in C, but C is nothing like Java.

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What are strategies to get unstuck?

Lessons and ways in which programming in class is not like the real world.

Coding deliberately is important. Have a plan. Understand the existing code. Test assumptions. Don't code by trial and error.

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- Less code is better, and more likely to be correct.
- Reading code is as important and takes more time than writing code.

Approaches to Software Reliability

- Social
 - Code reviews
 - Extreme/Pair programming
- Methodological
 - Design patterns
 - Test-driven development
 - Version control
 - Bug tracking
- Technological
 - "lint" tools, static analysis
 - Fuzzers, random testing
- Mathematical
 - Sound type systems
 - Formal verification

Less "formal": Lightweight, inexpensive techniques (that may miss problems)

This isn't an either/or tradeoff... a spectrum of methods is needed!

Even the most "formal" argument can still have holes:

- Did you prove the right thing?
- Do your assumptions match reality?
- Knuth: "Beware of bugs in the above code; I have only proved it correct, not tried it."

More "formal": eliminate *with certainty* as many problems as possible.

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From: https://www.seas.upenn.edu/~cis500/current/lectures/lec01.pdf

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Strategies for debugging

Reduce to minimum example

- Check your assumptions.
- Use minimum example as basis for searching for help.

Debugging techniques

- ► Use assertions.
- ▶ Use debugging tools: Valgrind, Address Sanitizer, GDB.

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Use debugging printf statements.

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Programming assignment 2

- 1. Due Friday 2/23.
- 2. Graph algorithms and hash table.

Reading assignment: CS:APP Chapters 2.1, 2.2, 2.3

All about integers

- 1. We will launch in to our chapter on representing data in computers
- 2. First: all about integers, signs, capacities, operations.

bit bytes

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Why binary

Everything is bits

- Each bit is 0 or 1
- By encoding/interpreting sets of bits in various ways
 - Computers determine what to do (instructions)
 - ... and represent and manipulate numbers, sets, strings, etc...
- Why bits? Electronic Implementation
 - Easy to store with bistable elements
 - Reliably transmitted on noisy and inaccurate wires



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Decimal, binary, octal, and hexadecimal

Decimal	Binary	Octal	Hexadecimal	Decimal	Binary	Octal	Hexadecimal
0	<mark>0b0</mark> 000	000	0x0	8	0b1000	0010	0x8
1	0b0001	001	0x1	9	0b1001	0011	0x9
2	0b0010	002	0x2	10	0b1010	0012	0xA
3	0b0011	003	0x3	11	0b1011	0013	0xB
4	0b0100	004	0x4	12	0b1100	0014	0xC
5	0b0101	005	0x5	13	0b1101	0015	0xD
6	0b0110	006	0x6	14	0b1110	0016	0xE
7	0b0111	007	0x7	15	0b1111	0017	0xF

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In C, format specifiers for printf() and fscanf():

- 1. decimal: '%d'
- 2. binary: none
- 3. octal: '%o'
- 4. hexadecimal: '%x'

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= Z¹¹- (= Z02/f-) = Z047

 $z^{10} = (024)$ $z^{12} = 2040$ Base f $\frac{0}{512} \frac{1}{64} \frac{1}{8} \frac{1}{1}$ $0 \times 512 + (\times 64) + (\times 64) + (\times 64) + (\times 64)$ = 73

print ("Zodin, 090)

Decimal, binary, octal, and hexadecimal

How to represent the range of unsigned char in each?

Unsigned char is one byte, 8 bits.

- 1. decimal: 0 to 255 C 2. binary: 0b0 to 0b1111111 $256 1 = 2^{0} 1 = 0^{0} [00000000 0^{0} 0^{0}]$ 3. octal: 0 to 00377 (group by 3 bits) $= 0^{0} [11111 1^{0}]$ 3. octal: 0 to 0o377 (group by 3 bits)
- 4. hexadecimal: 0x00 to 0xFF (group by 4 bits) $\int_{22}^{10} \frac{3}{77} = \frac{162}{52}$



Often encountered use of hexadecimal: RGB colors

Red, green, blue values ranging from 0-255

C	<u> </u>		
#000000	#FFFFFF	#6A757C	#CC0033

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Representing characters

USASCII code chart

- char is a 1-byte, 8-bit data type.
- ASCII is a 7-bit encoding standard.
- "man ascii" to see 7,C Linux manual.
- Compile and run ascii.c to see it in action.
- Some interesting characters: 7 (bell), 10 (new line), 27 (escape).

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B7 D6 D	р ₇ b ₆ b ₅ ————				° ° 0	°°,	° ' 0	0 	¹ 0 ₀	¹ о	1 ₁	 	
- <u>'</u> .	Þ4 +	b 3 1	р ⁵	Ь ₁	Row	0	l	2	3	4	5	6	7
• •	0	0	0	0	0	NUL	DLE	SP	0	0	Р	``	P
	0	0	0	1	1	SOH	DC1	!	1	Α.	Q ·	0	P
	0	0	1	0	2	STX	DC2		2	B	R	b	r
	0	0	1	I	3	ETX	DC 3	#	3	C	S	C	S
	0	1	0	0	4	EOT	DC4	\$	4	D	Т	d	t
	0		0	1	5	ENQ	NAK	%	5	E	U	e	υ
	0	1	1	0	6	ACK	SYN	8	6	F	V	f	V
	0	Ι	1	1	7	BEL	ETB	,	7	G	¥	g	w
	1	0	0	0	8	BS	CAN	(8	н	X	h	×
	-	0	0	1	9	нт	EM)	9	1	Y	i	У
		0	1	0	10	LF	SUB	*	:	J	Z	j	Z
	1	0	1	1		VT	ESC	+		к	C	k j	(
	I	1	0	0	12	FF	FS	•	<	L	N	l	1
	1	1	0	1	13	CR	GS	-	ŧ.	м	כ	m	}
	1	1	1	0	4	SO	RS		>	N	^	n	\sim
	-1				15	S 1	US	1	?	0		0	DEL

Figure: ASCII character set. Image credit Wikimedia

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- Network and UNIX settings using bit masks (e.g., umask)
- Hardware and microcontroller programming (e.g., Arduinos)
- Instruction set architecture encodings (e.g., ARM, x86)

Bitwise operations

~: bitwise NOT

Siturise operations
i.i. bitwise NOT
unsigned char a = 128

$$a = 0b1000_0000 = 125$$

 $a = 0b1000_0000 = 125$
 $a = 0b1000_0000 = 125$

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= 127

Bitwise operations		printf (god/n,	38	1	ز(
		3=> 0600011			
& hitwise AND	đ	1=> 060000			
		06 000 01	a	b	a & b
			0	0	0
3&1 = 0b11&0	b01		0	1	0
-0b01			1	0	0
- 0001			1	1	1

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Bitwise operations

Z=> 060011 1 => 060001 ^: bitwise XOR a^b b а 0 0 0 $3 \wedge 1 = 0b11 \wedge 0b01$ 0 1 1 0 100 90 0 1 1 = 0b100 1 1 = 2

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inplaceSwap.c: Swapping variables without temp variables.

y = (X 1 4) > =) $X = X \wedge (\frac{1}{2} = X \wedge (X \wedge Y) = (X \wedge X) \wedge Y$ $\Rightarrow j: \times \land y;$ = 0x y = y; = YA(XAY); $= \eta \wedge (\eta \wedge \times);$ $X \subset Y$; $= (\eta \Lambda \eta) \Lambda \chi$ Y<= X ; $= 0 \Lambda \chi$ = X 5

How does it work?

Don't confuse bitwise operators with logical operators

Bitwise operators



Logical operators









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Ways to represent negative numbers

- 1. Sign magnitude
- 2. 1s' complement
- 3. 2's complement

Representing negative and signed integers

Sign magnitude Flip leading bit.



Representing negative and signed integers

1s' complement

- ► Flip all bits
- Addition in 1s' complement is sound
- In this encoding there are 2 encodings for 0

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- ► -0: 0b1111
- ► +0: 0b0000

Representing negative and signed integers 2's complement

signed char	weight in decimal
0000001	1
00000010	2
00000100	4
00001000	8
00010000	16
00100000	32
01000000	64
1000000	-128

Table: Weight of each bit in a signed char type

- what is the most positive value you can represent? 127
- what is the most negative value you can represent? -128
- ▶ how to represent -1? 1111111
- ▶ how to represent -2? 11111110

Representing negative and signed integers 2's complement

signed char	weight in decimal
0000001	1
00000010	2
00000100	4
00001000	8
00010000	16
00100000	32
0100000	64
1000000	-128

Table: Weight of each bit in a signed char type

► MSB: 1 for negative

- ► To make a number negative: flip all bits and add 1.
- Addition in 2's complement is sound

Importance of paying attention to limits of encoding



Figure: Image credit: CS:APP



Figure: Image credit: CS:APP

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Importance of paying attention to limits of encoding



Figure: Image credit: CS:APP

Figure: Image credit: CS:APP

https://www.theatlantic.com/technology/archive/2014/12/ how-gangnam-style-broke-youtube/383389/

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Programming assignment 2: Graphs, trees, queues, hashes

Programming Assignment 2 parts

- 1. edgelist: loading and printing a graph
- 2. isTree: needs either DFS (stack) or BFS (queue)
- 3. mst: a greedy algorithm
- 4. solveMaze: needs either DFS (stack) or BFS (queue)
- 5. findCycle: needs either DFS (stack) or BFS (queue)

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6. hashTable: a separate chaining hash table

Using graphutils.h

The adjacency list representation

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- The edgelist representation
- ► The query

Binary search tree



Figure: BST with input sequence 7, 4, 7, 0, 6, 5, 2, 3. Duplicates ignored.

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Binary search tree level order traversal



Figure: Level order, left-to-right traversal would return 7, 4, 0, 6, 2, 5, 3.

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Binary search tree traversal orders

Breadth-first

- ► For example: level-order.
- Needs a queue (first in first out).
- ► Today in class we will build a BST and a Queue.

Depth-first

► For example: in-order traversal, reverse-order traversal.

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Needs a stack (first in last out).

typedef

Why types are important

Natural language has nouns, verbs, adjectives, adverbs.

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- ► Type safety.
- Interpretation vs. compilation.

```
typedef struct BSTNode BSTNode;
struct BSTNode {
    int key;
    BSTNode* l_child; // nodes with smaller key will be in left s
    BSTNode* r_child; // nodes with larger key will be in right s
};
```

```
// queue needed for level order traversal
typedef struct QueueNode QueueNode;
struct QueueNode {
    BSTNode * data;
    QueueNode* next; // pointer to next node in linked list
};
typedef struct Queue {
    QueueNode* front; // front (head) of the queue
    QueueNode * back; // back (tail) of the queue
} Queue;
```

Let's implement enqueue ()

https://visualgo.net/en/queue

- ► First, consider if queue is empty.
- Then, consider if queue is not empty. Only need to touch back (tail) of the queue.

Let's implement dequeue ()

https://visualgo.net/en/queue

- ► First, consider if queue will become empty.
- Then, consider if queue will not not empty. Only need to touch front (head) of the queue.

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Subtle point: why are the function signatures (return, parameters) of enqueue() and dequeue() the way they are?